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Total No. of Questions: 9]

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# B.Tech. (Sem. - 1<sup>st</sup>/2<sup>nd</sup>)

# **ENGINEERING MATHEMATICS - I**

**SUBJECT CODE**: AM - 101 (2K4 & ONWARDS)

Paper ID : [A0111]

[Note: Please fill subject code and paper ID on OMR]

Time: 03 Hours

Maximum Marks: 60

# **Instruction to Candidates:**

- 1) Section A is Compulsory.
- 2) Attempt any Five questions from Section B & C.
- 3) Select atleast two questions from Section B & C.

#### Section - A

*Q1)* 

[Marks: 2 each]

- a) Test for the convergence of the series  $\sum \left(\frac{n}{n+1}\right)^{n^2}$ .
- b) Using double integration, find area enclosed between the curves  $y^2 = x^3$  and x = y.
- c) If  $u = x^3 + xy$  and v = xy. Find  $\frac{\partial(u, v)}{\partial(x, y)}$ .
- d) Prove  $\Gamma(n+1) = n\Gamma(n)$ , where n > 0.
- e) Find the curvature of curve  $y^2 = x^3 + 8$  at the point (1, 3).
- f) Find the cube roots of unity.
- g) Evaluate  $\int_0^2 \int_1^2 \int_0^{yz} xyz \ dxdydz$ .
- h) Define homogeneous function with an example.
- i) Find the centre and the radius of the sphere  $x^2 + y^2 + z^2 6x + 8y 10z + 1 = 0$ .
- j) Expand  $\tan x$  in powers of x upto  $x^3$ .

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### Section - B

[Marks: 8 Each]

- Q2) (a) State and prove Euler's theorem.
  - (b) If  $z = \sqrt{x^2 + y^2}$  and  $x^3 + y^3 + 3axy = 5a^2$ , find the value of  $\frac{dz}{dx}$ , when x = y = a.
- **Q3)** (a) Trace the curve  $a^2y^2 = x^2(a^2 x^2)$ .
  - (b) If  $\rho_1, \rho_2$  be the radii of curvature at the extremities of the chord of the cardioid  $r = a(1 + \cos \theta)$  which pass through the pole, show that  $\rho_1^2 + \rho_2^2 = \frac{16a^2}{9}.$
- **Q4)** (a) Expand  $x^2y + 3y 2$  in powers of (x 1) and (y + 2) using Taylor's theorem.
  - (b) Discuss maxima and minima of  $x^3y^2(1-x-y)$ .
- **Q5)** (a) Find the moment, about x-axis of arc of parabola  $y = \sqrt{x}$ , lying between (0, 0) & (4, 2).
  - (b) Find root mean square of  $\sin x$  over the range x = 0 to  $\pi/2$ .

## **Section - C**

[Marks: 8 Each]

**Q6)** (a) Show that the two circles  $x^2 + y^2 + z^2 - 2x + 3y + 4z - 5 = 0$ , 5y + 6z + 1 = 0

 $x^2 + y^2 + z^2 - 3x - 4y + 5z - 6 = 0$ , x + 2y - 7z = 0lie on the same sphere and find its equations.

- (b) Find the equation of cone whose vertex is at the points (1, 1, 3) and which passes through the ellipse  $4x^2 + z^2 = 1$ , y = 4.
- **Q7)** (a) Change the order of integration  $\int_0^1 \int_{x^2}^{2-x} xy \ dxdy$  and hence evaluate the integral.
  - (b) Prove that  $\int_{1}^{0} \frac{x \, dx}{\sqrt{1-x^5}} = \frac{1}{5} \beta \left(\frac{2}{5}, \frac{1}{2}\right)$ .

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- **Q8)** (a) Test the convergence of the series  $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5} + \dots$ 
  - (b) Show that the series  $\sum_{n=1}^{\infty} \frac{\sin(x^2 + nx)}{n(n+2)}$  for all real x, is uniformly convergent.
- **Q9)** (a) Separate  $tan^{-1}(x + iy)$  into real and imaginary parts.
  - (b) Solve the equation  $x^4 x^3 + x^2 x + 1 = 0$ , using De Moivre's theorem.

